

Shape and appearance models of talking faces for model-based tracking

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Abstract

This article presents a system that can recover and track the 3D speech movements of a speaker’s face for each image of a monocular sequence. A speaker-specific face model is used for tracking: model parameters are extracted from each image by an analysis-by-synthesis loop. To handle both the individual specificities of the speaker’s articulation and the complexity of the facial deformations during speech, an accurate 3D model of the face geometry and an appearance model are built from real data. The geometric model is linearly controlled by only seven articulatory parameters. Appearance is seen either as a classical texture map or through local appearance of a relevant subset of 3D points. We compare several appearance models: they are either constant or depend linearly on the articulatory parameters. We evaluate these different appearance models with ground truth data.

1. Introduction

For most applications for communication that involve virtual talking faces, high fidelity is required when re-synthesizing facial movements, and thus for their prior extraction. Tracking speech movements in a video is a challenging task because expected reconstruction results must be very accurate.

In this article, we have in mind virtual teleconferencing applications: in a common virtual space, every participant is represented by a 3D delegate reproducing the gestures of his/her owner. We face the problem of robustly recovering the 3D speech movements of a given speaker from monocular images.

To achieve such tasks, making use of a 3D face model is a very popular approach. Generic 3D models can be classified as parametric [1][2] or physics-based [3] [4]. These *a priori* models must be customized to the anatomy of the speaker before tracking his/her facial movements. Even then, it is not guaranteed that they could be fairly adapted to every facial configurations. Data driven models can cope with this problem [5][6] [7]. We will describe below a methodology that lets control parameters of a speaker-specific model emerge from a statistical analysis of fine-grained 3D data.

With only a 3D model, low-level image processing techniques are usually employed to extract the positions in the image of features such as interest points, gradient, or edges [8][9]. Then, these 2D measurements must be inverted to determine the control parameters of the 3D model: this operation may be an *ill-posed* problem as the solution may not exist, or may not be unique. Because optical flow generates a large number of correspondences, the inversion is more likely to lead to a solution [10]. It can be combined with edge-adjustment [11], or with analysis-by-synthesis technique [12].

Face images depend on head motion, illumination conditions and facial movements. In presence of large image changes, tracking can take great advantage of an appearance-variations model, which is moreover included in an analysis-by-synthesis loop. This has been successfully applied for recovering head pose [13], expressions [14], or identity [15].

As we concentrate on speech movements, we assume small head motion and small illumination variations. Following our 3D modelling methodology, we use statistical analysis to build the appearance models. They are linearly controlled by the same articulatory parameters that drive the geometric model. In addition to classical texture mapping of the whole face, model of local appearance of a subset of relevant 3D points is also implemented.

Our 3D geometric model is presented in next section. The appearance models are described in section 3. Then, the tracking stage is detailed and finally results of several experiments are discussed.

2. 3D Geometric model

The geometric model of the speaker’s facial movements is 3D, linear and driven by a vector α of seven articulatory parameters. A translation \mathbf{t} and a rotation \mathbf{R} define the global head motion which frames the speech movements. Finally, the 3D face model is entirely controlled by the set of parameters p :

$$p = [\alpha^T \quad t_x \quad t_y \quad t_z \quad r_x \quad r_y \quad r_z]^T$$

We follow our well-experienced methodology, presented with more details in [16, 17]; constructing an articulatory model specific to the speaker so as to capture its audiovisual speech activity comprises two stages: collecting accurate 3D data of the speaker and analysing them through a statistical iterative scheme.

2.1. Data acquisition

As shown in figure 1, glued coloured beads mark a few hundreds fleshpoints all over the speaker’s face. Using calibrated cameras and mirrors, we record a corpus composed of:

- the french oral and nasal vowels { i, e, ε, a, o, u, y, ø, œ, ā, ē, ̃, œ̃ };
- a set of central realisations of VCV triphones, where C is one of { i, e, a, o, u, œ } and V is one of { p, t, k, b, d, g, f, v, s, z, ʃ, ʒ, ʁ, l, m, n, ð, θ };
- two *silent* postures: *rest* (closed mouth) and *preph* (mid-opened mouth).

On each of these visemes, the 3D coordinates of each fleshpoint and of 30 points characterizing lips shape ([17]) are then reconstructed and expressed in a referential linked to the bite plane.



Figure 1: Data acquisition setup. Speaker uttering /iki/

2.2. Data modelling

The 3D linear model emerges from iterative statistical analysis of these 3D data. Here, we only consider a subpart of the corpus: the model is built from a collection of 275 3D points for 68 visemes. Successive applications of Principal Component Analysis are performed on selected points. They generate the main directions that are retained as *linear predictors* for the whole data set. At each step of the model construction, action of the *current* parameter is determined by explaining the residual data with the following predictors:

1. jaw1: y-coordinates of jaw line points and lower teeth
2. lips1: xyz-coordinates of lips points and lips-contouring beads points
3. lips2: y-coordinates of lower lip points and lower lip-contouring beads points
4. lips3: y-coordinates of upper lip points and upper lip-contouring beads points
5. lips4: y-coordinates of lips points and lips-contouring beads points
6. jaw2: z-coordinates of jaw line points and lower teeth
7. lar1: xyz-coordinates of all points except lips and lower teeth

That way, facial speech movements are hence linearly controlled by seven non-orthogonal parameters, according to:

$$X = [x_1 \ y_1 \ z_1 \ \dots \ x_n \ y_n \ z_n]^T = X_0 + M_X \cdot \alpha$$

As summarized in table 1, the articulatory model explains more than 96% of the data variance. It can reproduce trustfully the geometry of the visemes: figure 2 shows that the modelling error is around a half millimeter for most visemes. The worst-modellized visemes are the two *silent* postures (*preph* and *rest*) and /œθœ/ (the subset corpus has no triphones with /œ/ nor /θ/). The worst-modellized points belongs to the inner lip contour: it is quite ill-defined to truly anchor fleshpoints on it.

jaw1	16.11	(16.11)
lips1	50.10	(66.21)
lips2	10.19	(76.40)
lips3	9.60	(86.00)
lips4	6.72	(92.72)
jaw2	1.60	(94.33)
lar1	1.96	(96.29)

Table 1: Contribution of each articulatory parameter (and cumulated sum) to data variance reduction (in %).

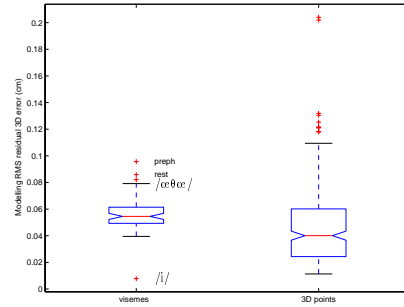


Figure 2: Boxplots of the direct inversion of the 3D model on its learning data

This construction paradigm keeps the advantages of data-driven techniques while producing somewhat comparable results with our previous six-parameters controlled clones [18]. Whereas instructed to utter neutral speech, the speaker has sometimes smiled during the recording session: we have had to introduce the parameter lips4 so as the other parameters could keep clear a *posteriori* phonetic interpretations (see figure 3).

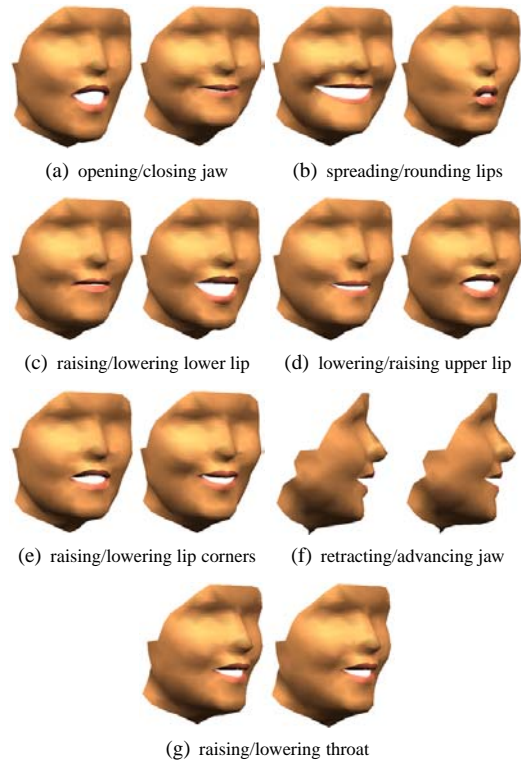


Figure 3: The elementary movements of the articulatory model. From (a) to (g): Nomograms of jaw1, lips1, lips2, lips3, lips4, jaw2 and lar1.

3. Appearance models

Thanks to the accuracy of the geometric model, it is likely that, for fine 3D tracking purpose, the appearance model needs only

to bring *few information* so that the tracking algorithm produces satisfying results. As we assume small head motion and small illuminating changes, applying here widely used techniques based on appearance eigenspaces [6][15][19] would just complexify the task: it would add to the face model appearance parameters that would have to be mapped to the shape parameters.

The two different appearance models detailed below depend linearly on the articulatory parameters; linked to shape changes, appearance changes can be reinterpreted into facial movements.

3.1. Texture mapping (tex)

Assuming an image, a texture I can be defined by a set of control parameters p . Warping the geometry to a given posture (corresponding to p_0) allows to warp I to a normalized-shape image referential. Its dimensions are constant and depend only on p_0 . In this referential, a variable texture is modelled as:

$$I_{tex} = [R_1 G_1 B_1 \dots R_m G_m B_m]^T = I_0 + \mathbf{M}_I \cdot \alpha \quad (1)$$

For synthesis of the face, I_{tex} is computed and serves as texture for the morphed 3D posture. Projection onto the image plane finally leads to a set \mathcal{S} of *rendered* pixels.

As an example, such a model was learned on visemes used for the geometric modelling. Due to the variations of head motion, slight light variations and the warping noise, it explains only 56% of the RGB data variance. However, as illustrated in figure 4 (and in figure 6 for tracking) it renders properly the major appearance changes, such as the different aspects of the nasogenian wrinkle for spread or rounded lips.



Figure 4: Synthesis of normalized-shape textures. Nomo-grams of jaw1 (left) and lips1 (right).

3.2. Model of local appearance (la)

A marker-free face contains large parts where the texture is very poor and not subject to major variations. It seems then interesting to model appearance only for the more informative regions. We do so by modelling the local appearance of selected 3D points.

We describe the local appearance with a vector d containing responses to Gaussian derivative filters [20].

The following is illustrated on figure 5. For a 3D point, the convolutions are computed at its projection (u, v) on the image I . To ease the dissociation between luminance and chrominance, image values $I(u, v)$ are expressed in the colour space (Y, C_b, C_r) :

$$\begin{pmatrix} Y \\ C_b \\ C_r \end{pmatrix} = \begin{pmatrix} 0.2220 & 0.7067 & 0.0713 & 0 \\ -0.1195 & -0.3805 & 0.5000 & 127.5 \\ 0.5000 & -0.4542 & -0.0458 & 127.5 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \\ 1 \end{pmatrix}$$

To approximate the local image variation, up to the first Gaussian derivatives are represented in d ; the zeroth order derivative of the Y channel is discarded so that d is not sensitive to luminance offset changes; this leaves eight components for d :

$$d = \begin{pmatrix} Y \\ C_b \\ C_r \end{pmatrix} \star (G_0(\sigma_0) \quad G_1^x(\sigma_0) \quad G_1^y(\sigma_0)) \setminus \{Y_{G_0(\sigma_0)}\}$$

where the convolutions are computed at a scale σ_0 , which is kept constant in this article.

As can be seen on figure 5, local appearance depends on the articulatory gesture. The contrast rounded/spread lips changes the gradient orientation near lip corners. The neighbourhood of a point belonging to inner contour is sensible to lips aperture.

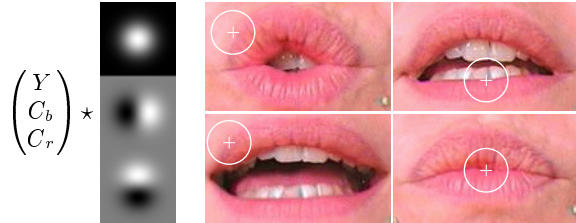


Figure 5: Computing local appearance. Left: the Gaussian derivative filters applied on each of the Y , C_b and C_r channels. Right: difference in articulation induces changes of appearance.

Again, for each point P^i of the 3D model, d^i is linearly modelled by the articulatory parameters:

$$d^i = d_0^i + \mathbf{M}_D^i \cdot \alpha \quad (2)$$

For each articulatory parameter, a few points are automatically selected according to a criterion of the variance of the data reconstructed by the corresponding column of \mathbf{M}_D^i . Duplicates are removed when merging into the final set.

Finally, appearance of the face is defined as a set of N 3D points local appearance:

$$\mathbf{D} = [d^1 \quad d^2 \quad \dots \quad d^N] \quad (3)$$

Texture-mapping appearance model can also be formalized in (3): then, N is the cardinal of \mathcal{S} , and each descriptor d^i is a vector containing the luminance-normalized RGB values (*i.e.* divided by $L = R + G + B$) of the i^{th} pixel of \mathcal{S} .

There are several important differences between these two appearance models.

Image distortion. Whereas the texture mapping approach involves an important distortion due to the warping stage, the model of local appearance is quite view-dependent.

Context sensitiveness. Contiguous facets of the mesh may behave rather differently whereas the local appearance integrates changes in a neighbourhood, which allows for example to distinguish between lips and inner mouth for closed/opened lips.

Registration. Model of local appearance may rely initially on intensive tracking of a few interest points that can be automatically augmented as the system gain in robustness and precision:

bootstrapped with lip corners and lip contours, it may register additional points on the skin and may even lead eventually to a linear texture model.

4. Tracking algorithm

The face model described in sections 2 and 3 permits to synthesize a set of appearance descriptors \mathbf{D}^s that corresponds to a vector of control parameters p . Our fitting algorithm performs the inverse task: it aims to recover the parameters \hat{p} which synthesizes the descriptors $\hat{\mathbf{D}}^s$ that best match the descriptors \mathbf{D}^a of the analysed image I^a . The dissimilarity between parameters p and image I^a is measured as the distance between the descriptors \mathbf{D}^s and \mathbf{D}^a :

$$\varepsilon(p) = \frac{1}{NN_d} \sum_{i=1}^N \sum_{j=1}^{N_d} (D_{i,j}^a(p) - D_{i,j}^s(p))^2 + A(\alpha)$$

where N_d -coordinates $D_{i,j}^a(p)$ and $D_{i,j}^s(p)$ are computed according to section 3, and $A(\alpha)$ is an exponentially-fashioned function that penalizes improbable articulatory parameters.

The purpose of our analysis-by-synthesis optimization scheme is to deliver: $\hat{p} = \arg \min_p \varepsilon(p)$

We have compared several classical optimization methods, including Levenberg-Marquardt and local variations. The best convergence results were obtained by the Nelder-Mead downhill simplex algorithm [21].

For sequence tracking, the best fitting parameters for a given image are used as the initial simplex centroid for the following one.

5. Objective evaluations

The goal of the experiments detailed below is both to evaluate our system and to compare the different appearance models on ground truth data. These ground truth data were obtained by computing a direct inversion of the geometric model from semi-automatically labelled positions of glued beads. Cameras were calibrated in all experiments.

5.1. Validation experiments

For the following experiments, the tracking system was evaluated in the geometric modelling conditions. Out of the four views of the setup (see figure 1), only one front view was used.

The visemes used for the construction of the geometrical model have been randomly separated in two classes: 80% of the visemes have been dedicated to the construction of the appearance models, and 20% have been kept apart for the tests.

We have built four appearance models: texture mapping models `tex_lin` and `tex_cst` are controlled according to (1), `tex_cst` doesn't vary with α ($M_I = 0$); similarly, the models of local appearance `la_lin` and `la_cst` are controlled according to (2), `la_cst` doesn't vary with α ($M_D^I = 0$). They use $N = 63$ 3D points.

The first tracking experiment was performed on the tests visemes. Head motion was precisely estimated during the construction of the geometric model, and only articulatory parameters were tracked, using the neutral posture as the initial conditions. Figure 6 shows the residual 3D error computed including all the 3D points of the geometric model. With appearance models `tex_lin`, `tex_cst` and `la_lin` the system quite successfully recovers the geometry of the visemes. A large part of the visemes have residual 3D error below the uncertainty of the geometric

modelling. Results with `tex_lin` and `la_lin` are better than those with `tex_cst` and `la_cst`, showing the benefit of the articulatory-dependent modelling. Some failures, such as for /asa/, have occurred; however, the tracking was initialised far from the solution: when tracking a sequence, only few variations have to be estimated between two successive frames.

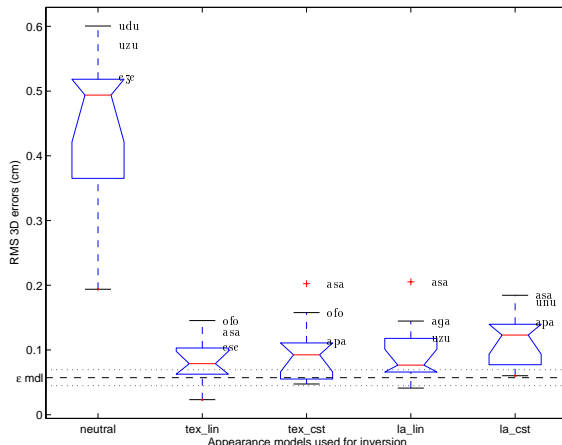


Figure 6: Boxplots of the tracking residual RMS 3D error on test visemes for different appearance models. For each group, the worst three visemes are labelled. For comparison, ‘neutral’ shows the initial error.

Another evaluation was performed by tracking both head motion and articulatory posture on an articulatory-balanced set of 77 test sentences. This experiment involves a total of 7546 frames; models trainings use 68 visemes.

The figure 8 illustrates the tracking results for the sentence “massue”. Best results are obtained with `tex_lin`; `tex_cst` and `la_lin` behave equally well; `la_cst` is clearly worse. The geometric measurements lip width and lip aperture allow to see that the estimated articulatory movements reproduce the anticipatory gestures and reach *phonetic* targets such as lips closure for the bilabial stops /p/ and /m/. On average, the error function is called around 300 times per frame upon convergence, mainly because we have kept the very conservative ending criteria used when tracking the visemes.

Results of the tracking with `tex_cst` of all the sentences are illustrated in figure 7; a hierarchical cluster tree was constructed from the set of 3D coordinates corresponding to the acoustic realization centers of the phonemes. The distance between two groups was computed according to the median-modified Hausdorff distance. Quite similarly to [22], we retrieve for vowels a clear rounded/non-rounded distinction. Non-rounded vowels can be separated in two groups: {i, e, ε} and {a}. For consonants, we observe six groups; two for frontal articulations: bilabial {p, b, m} and labio-dental {f, v}; apico-dental articulations {t, d, n}; two for medium or back articulations: {ʋ, l} and the composite {s, z, k, g}; the rounded consonants {j, ʒ}.

Here, the beads glued on the whole speaker’s face enhance texture details; this bias yields great advantage to the texture-mapping models.

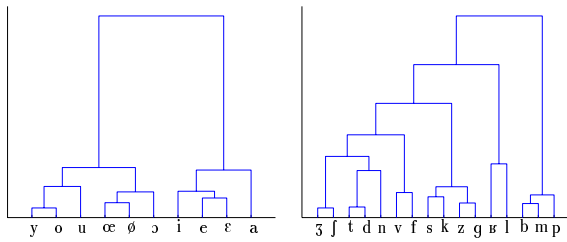


Figure 7: Geometric hierarchical clustering of the phonemes from the results of the 77 french sentences tracking with `tex_cst`. Scales for vowels and consonants are different.

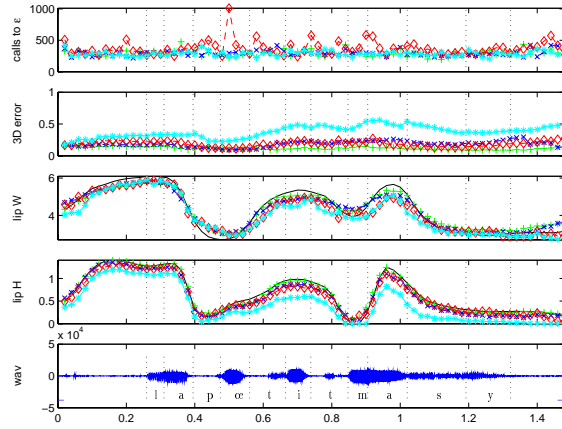


Figure 8: Tracking of the sequence “massue” with different appearance models. `tex_lin` (‘+’), `tex_cst` (‘x’), `la_lin` (‘◇’), `la_cst` (‘*’). Ground truth data is the solid line. From top to bottom: number of evaluations of ϵ , RMS 3D error (cm), lip width (cm), lip aperture (cm) and labelled audio.

5.2. Teleconferencing experiment

We now consider conditions that could be those of a real teleconference: the speaker is filmed by a single head-mounted calibrated micro-camera and his/her face is marked with only a few beads sufficient to compute reliably a direct inversion of the articulatory model (see figure 9). Note that the main region of interest — the lips — is left unmarked.

Data from a whole sequence was used for constructing the appearance models. We have only built the following models (denoted as above): `tex_cst` (first image of a sequence) and `la_lin` (using a whole sequence 75 images). They can both be computed very fast, either by graphical hardware for `tex_cst` or software for `la_lin`.

For the model of local appearance `la_lin`, 3D points in the neighborhood of a bead have been removed of the automatic selection process. The result shown in figure 9 makes sense: the $N = 51$ retained points are mainly distributed on lips and on the jaw line, including also a point located at the beginning of the nasogenian wrinkle.

These two appearance models have been tested by tracking the same sequence as used for the appearance models constructions (cf. figure 10). In this experiment, results with `la_lin` are much better than those with `tex_cst`. Average tracking resid-

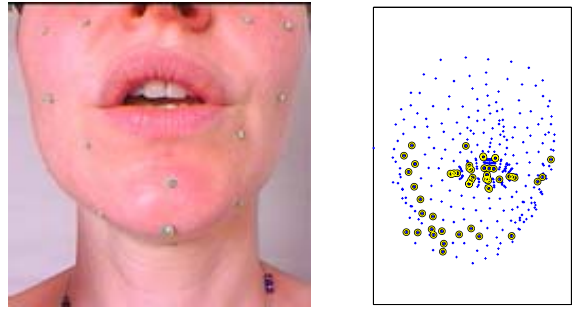


Figure 9: The corpus “annie”. Left: An image of the corpus. Right: Frontal view of the 3D points showing in big circles the points automatically selected for the model of local appearance.

ual RMS 3D error is 0.25 cm for `tex_cst` and 0.13 cm for `la_lin`. However, presence of peaks during the sequence indicate that even with the model of local appearance the tracking system could fail on a few frames (see figure 11).

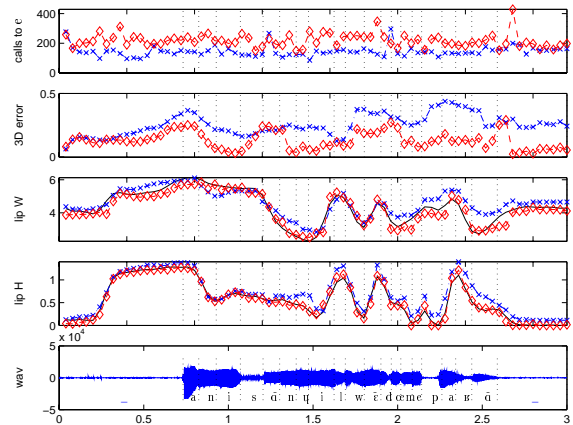


Figure 10: Tracking of the sequence “annie” with different appearance models. `tex_cst` (‘x’), `la_lin` (‘◇’). Ground truth data is the solid line. From top to bottom: number of evaluations of ϵ , RMS 3D error (cm), lip width (cm), lip aperture (cm) and labelled audio.

6. Conclusion

We have presented an original system to estimate the 3D speech movements of a speaker’s face for each image of a video. A speaker-specific face model is used for tracking: model parameters are extracted from each image by an analysis-by-synthesis loop. To capture the individual specificities of the speaker’s articulation, an accurate 3D model of the face geometry and an appearance model are built from real data. The geometric model is linearly controlled by only seven articulatory parameters. We have compared several appearance models, where appearance is seen either as a classical texture map or through local appearance of an automatically selected subset of 3D points. Evaluation with ground truth data has

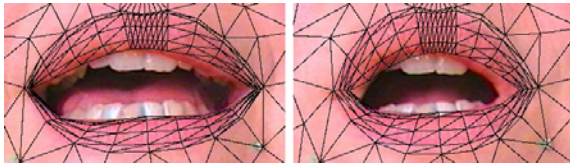


Figure 11: Examples of correct (left) and incorrect (right) la.lin model adjustment on images of the corpus “annie”.

shown satisfying results for the texture mapping models and for the model of local appearance linearly controlled by the articulatory parameters. This latter point allows to believe that our tracking system could reach real-time in a foreseeable future. Moreover, it can be completed with a module mapping facial speech movements to standardized MPEG-4 FAP [16] to form a working model-based encoder.

Further work will include extending the abilities of our tracking system and subjective evaluation.

To compute the local appearance, the Gaussian filters box is rigidly 2D. Deforming it by taking into account the corresponding 3D surface as in [23] is a step toward the construction of a new model of local appearance that would span several illuminating conditions. Also, each point should be considered at its intrinsic scale.

When tracking a sequence, a module for temporal prediction of the control parameters that includes audio information is under development.

Eventually, we plan subjective evaluation [24] of our tracking results by intelligibility tests. As what we have observed for geometrical confusions, we hope to retrieve the results of the literature, this time for perception. This will provide more clues for understanding how our virtual talking heads are perceived.

7. Acknowledgments

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